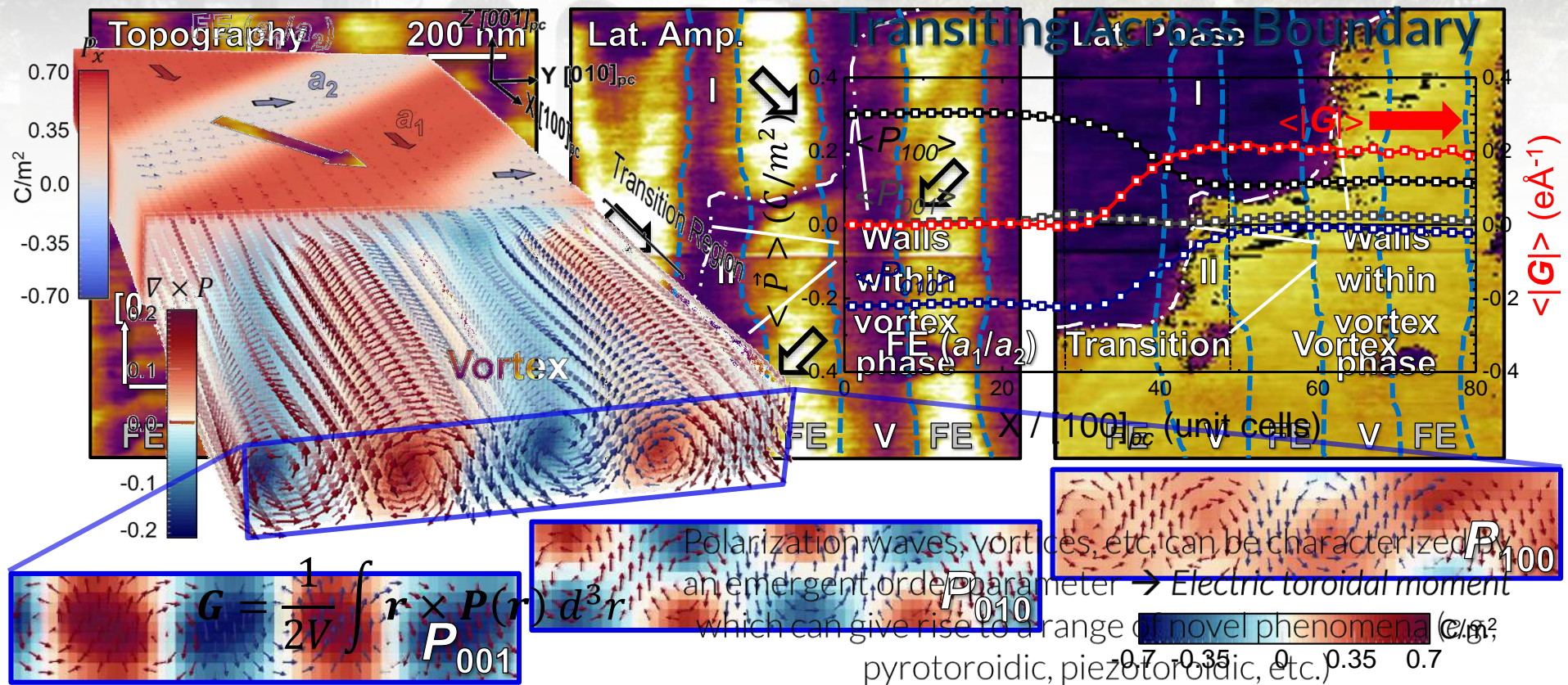


Emergent Toroidal Order



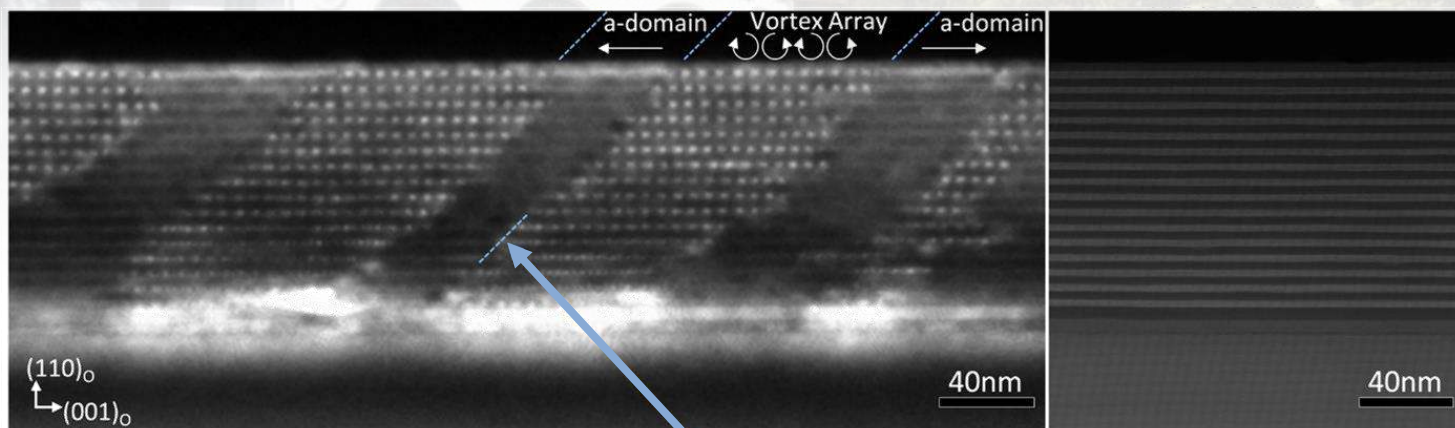
- Lateral PFM → 180° in-plane polarization change within vortex
- Phase-field → replicates coexistence
 - FE → Electric toroidal moment $\langle G \rangle = 0$, in-plane $P \neq 0$
 - Transition → ~20 UC, P rotation (Bloch-/Néel-like wall in FM), G increases
 - Vortex → G saturates to 0.2 e•Å⁻¹, arises from the continuous rotation of P , emergence of axial polarization component → **Electric toroidal phase**



Coexistence of Phases

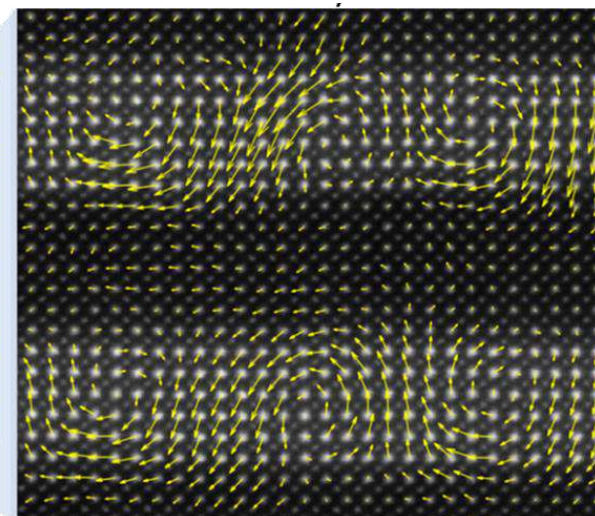
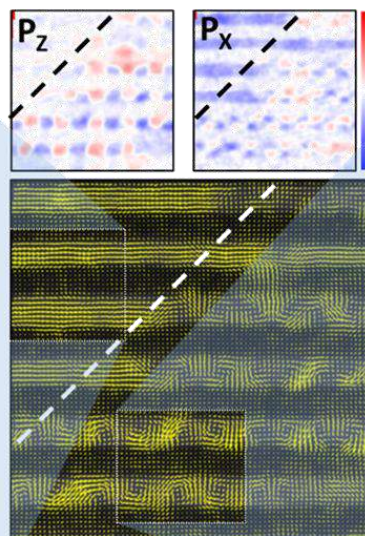
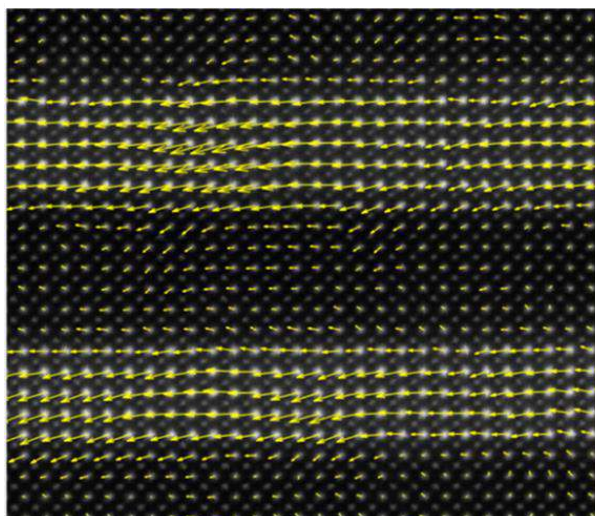
Dark-field TEM

HAADF STEM



a domain

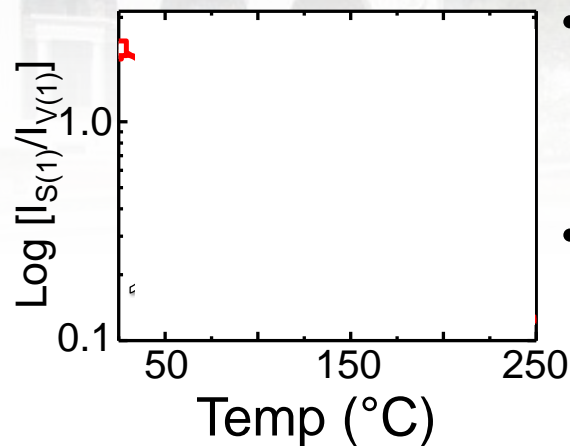
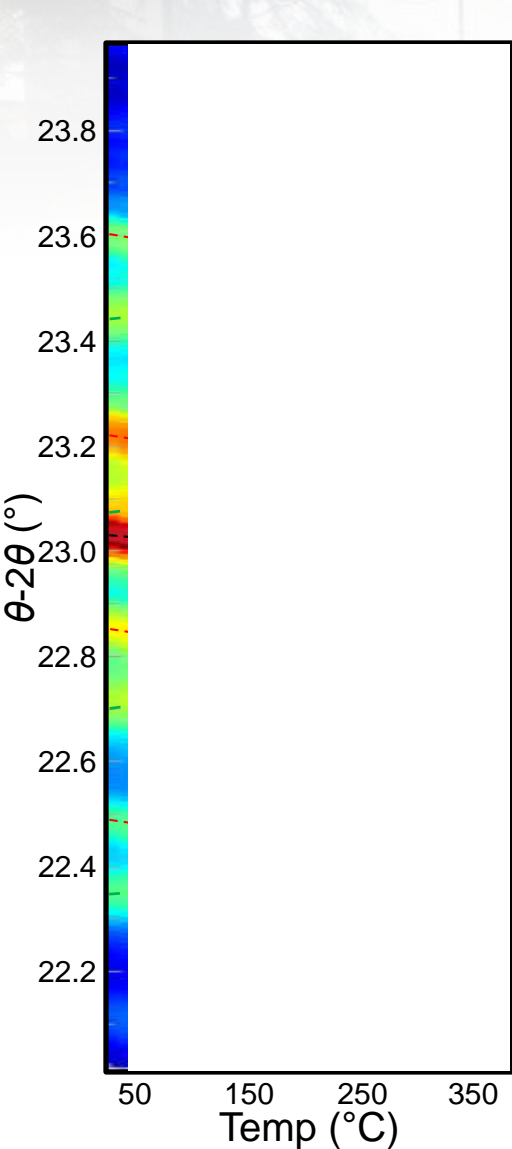
Vortex Array



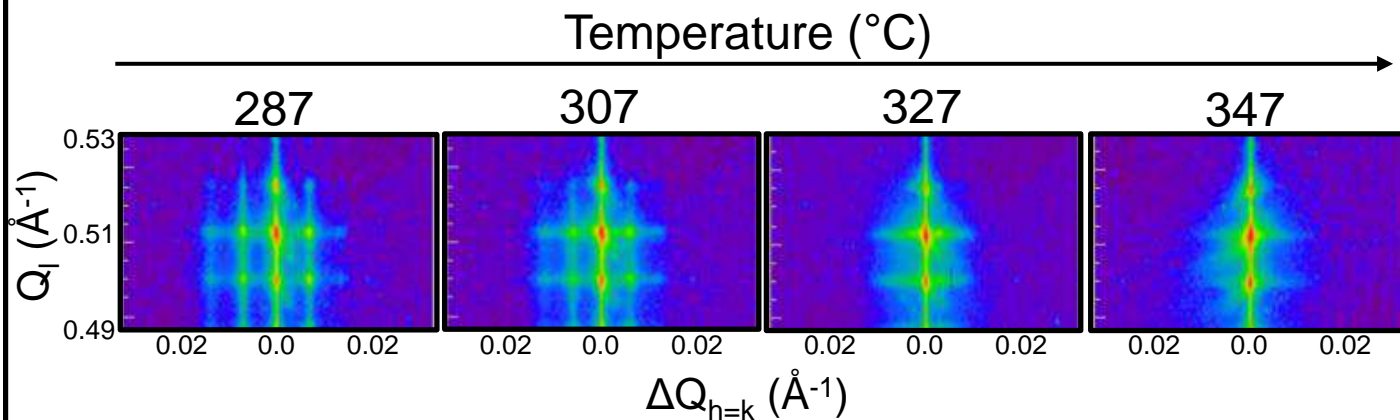
1st observation of toroidal and ferroic order co-existence



Phase Competition and Evolution: Temp.



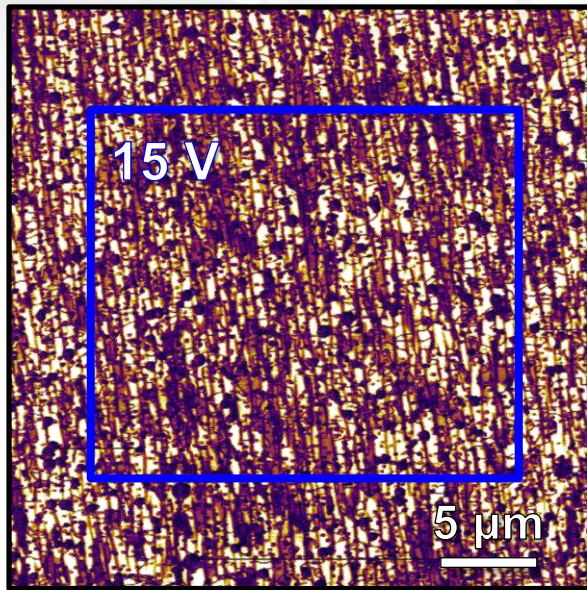
- *First-order phase transition* from toroidal to ferroelectric a_1/a_2 phase at $\sim 175^\circ\text{C}$
- Satellites from a_1/a_2 periodicity about 022-diffraction condition vanish at $\sim 327^\circ\text{C}$ \rightarrow FE to paraelectric transition



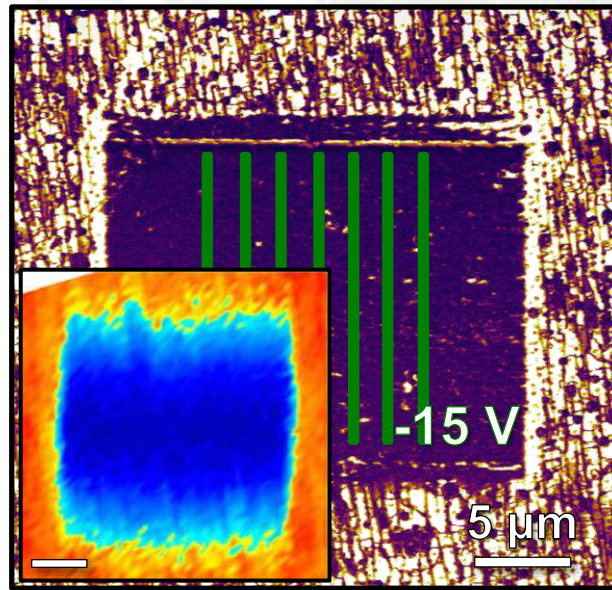
Phase evolution upon cooling:
PE \rightarrow FE (a_1/a_2) \rightarrow FE (a_1/a_2) + vortex (toroidal)
Vortex phase \rightarrow Exotic, glass-like transition

E-Field Control of Toroidal States

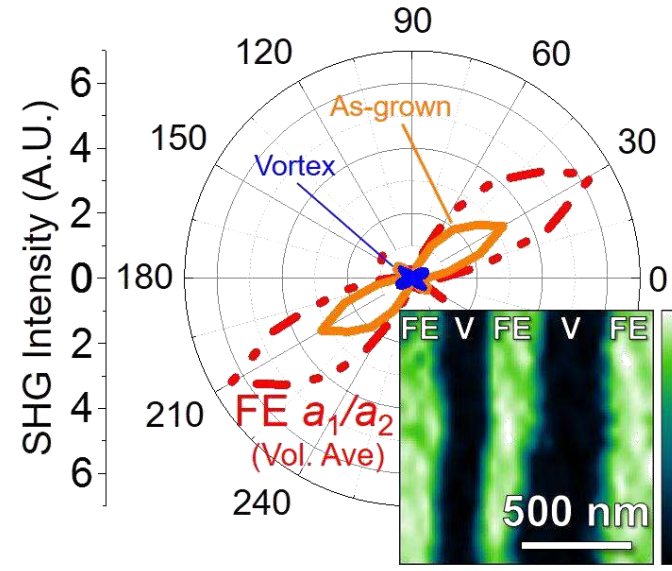
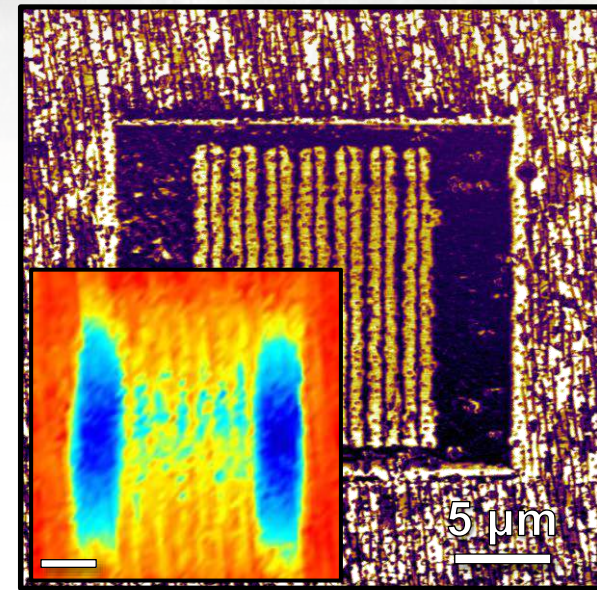
As-grown (Mixed Phase)



Poled to Vortex



Poled Back to Mixed Phase



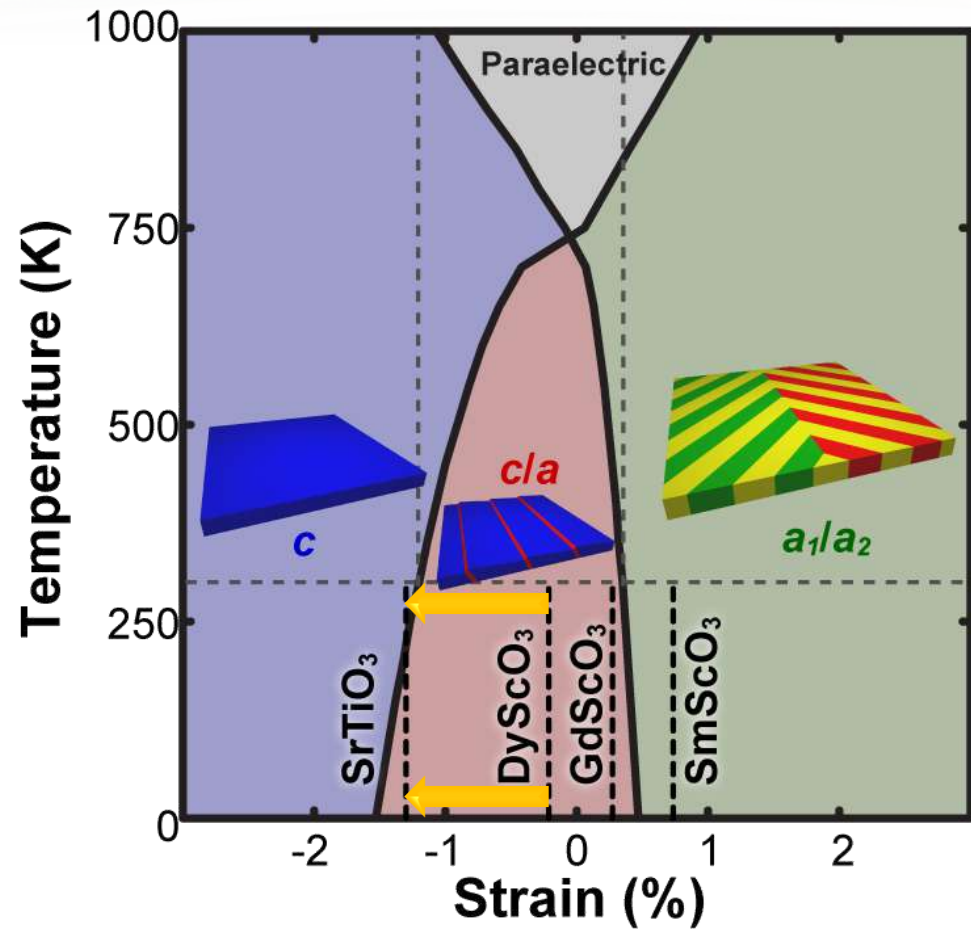
- +15V → Pure vortex
- -15 V → Mixed-phase
- X-ray microdiffraction → confirms reversible switching between phases
- Large changes in properties → Nonlinear optical properties dramatically different

E-field control of toroidal and ferroic order → New cross-coupled function



Controlling Emergent Structures

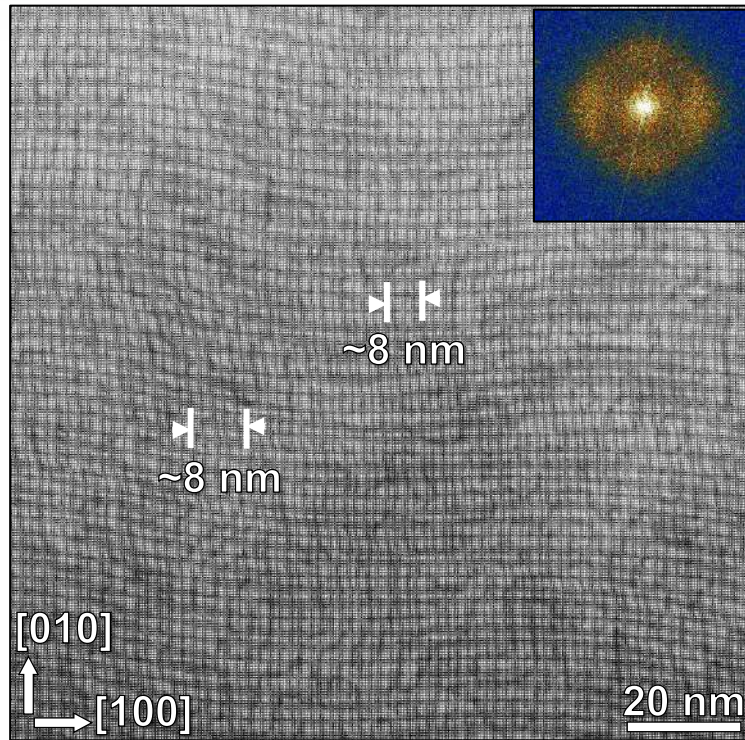
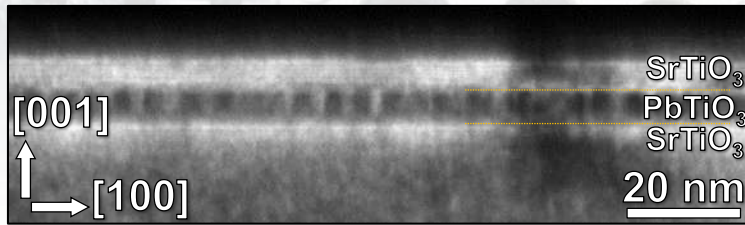
What happens if we change the strain in these superlattice structures? Can strain drive changes in the emergent order?



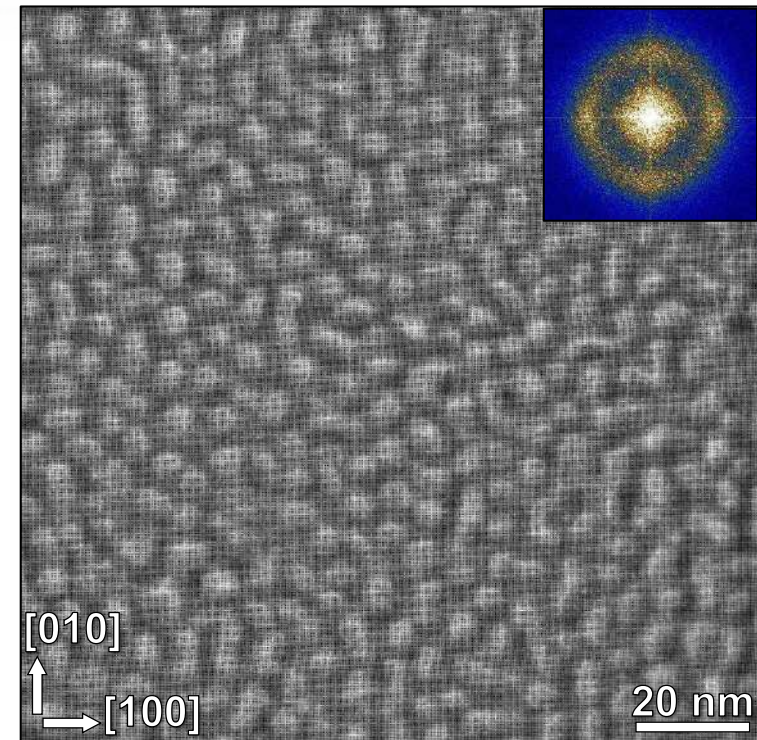
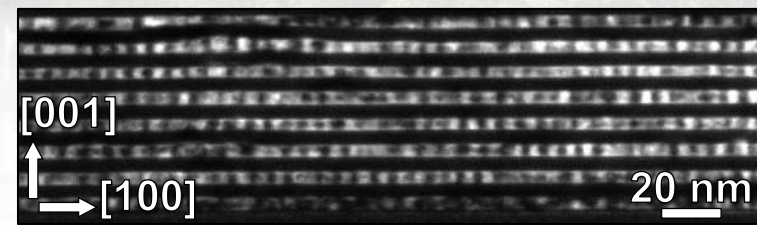


Controlling Emergent Structures

Trilayer
 $(\text{SrTiO}_3)_{16}/(\text{PbTiO}_3)_{16}/(\text{SrTiO}_3)_{16}$



Superlattice
 $(\text{SrTiO}_3)_{16}/(\text{PbTiO}_3)_{16} \times 8$



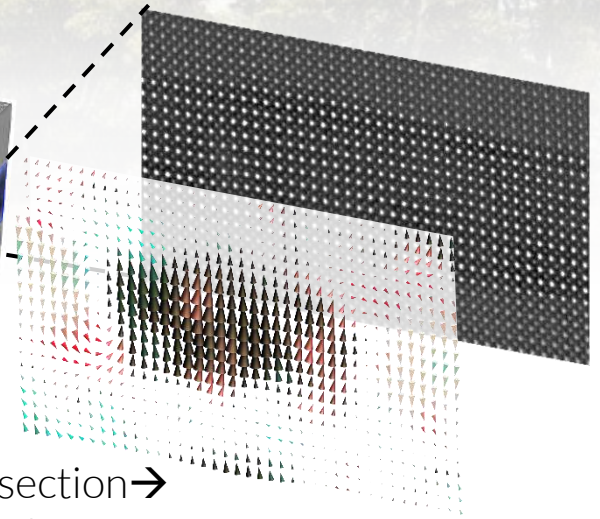
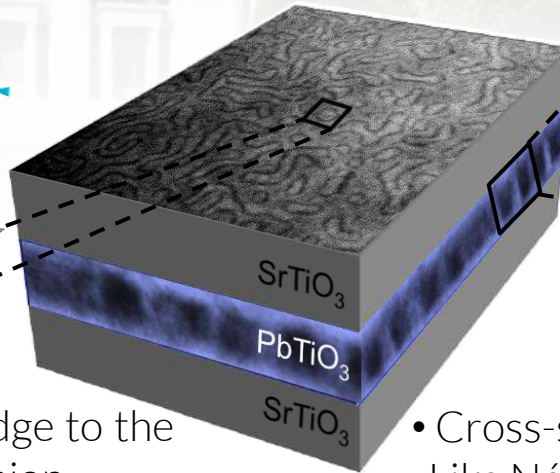
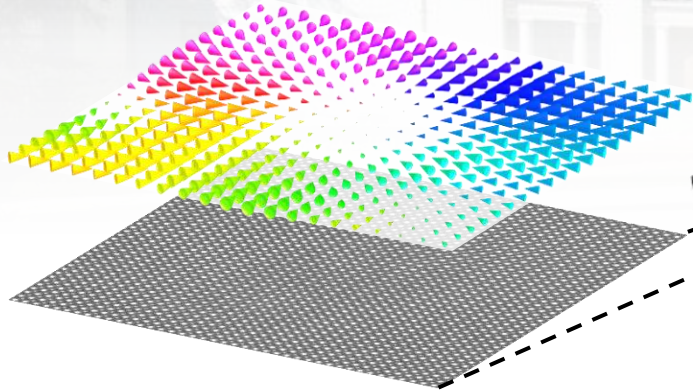
- New polarization morphologies → “Cheetos” and “bubbles”, length scale of ~8 nm, suggesting the formation of anti-parallel polar regions

What is the true structure of these new features?



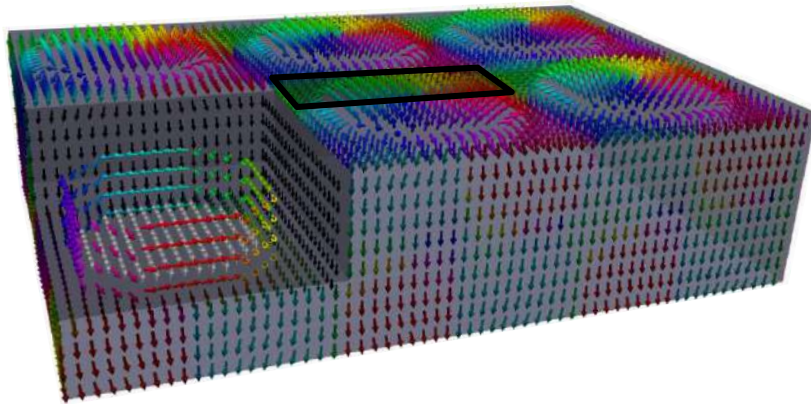
Understanding Emergent Structures

Atomic Polarization Mapping with STEM (NCEM)

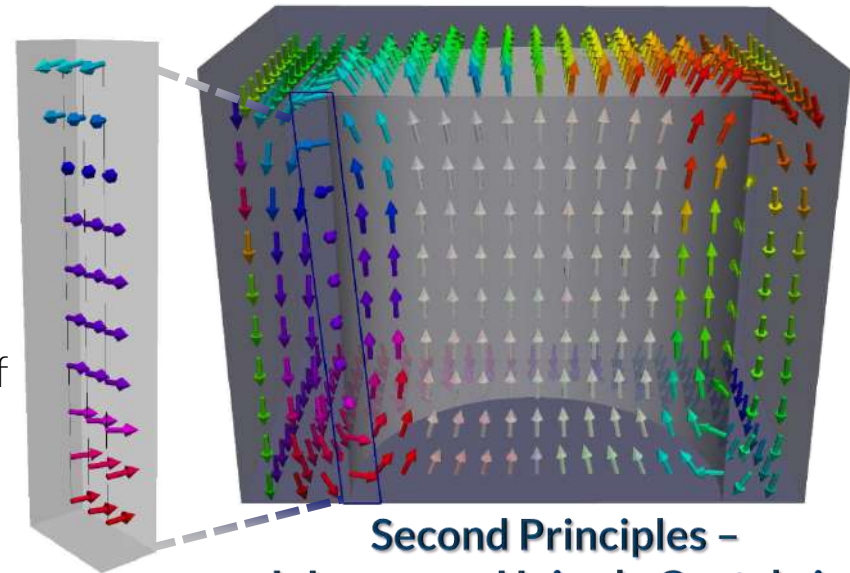


- Plan-view \rightarrow P converging from the edge to the center, reminiscent of hedgehog skyrmion

- Cross-section \rightarrow Like Néel skyrmion in FM; diverging and converging hedgehog skyrmion pair



- Second-principles calculations \rightarrow Confirm formation of polarization structures reminiscent of skyrmions
- Closer look \rightarrow Bloch-wall structure at mid-plane



Second Principles –
J. Junquera, Univ. de Cantabria

Skyrmions \rightarrow Integer topological number
Are these polarization structures truly skyrmions?

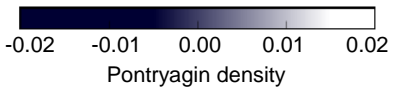
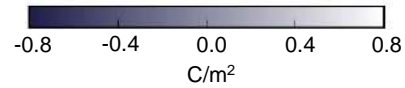
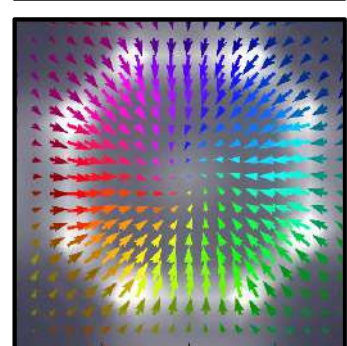
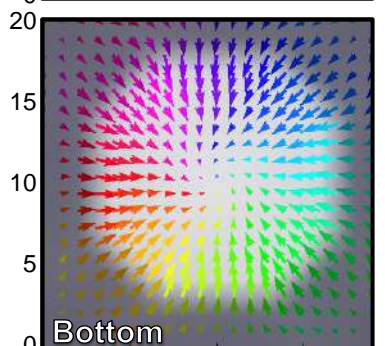
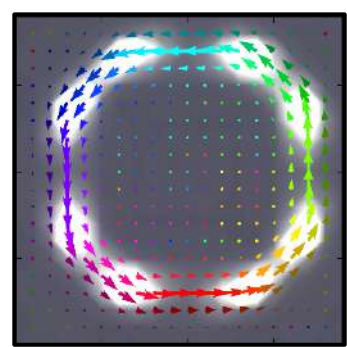
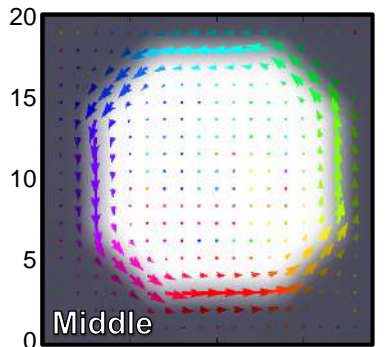
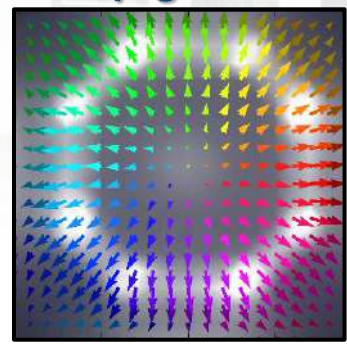
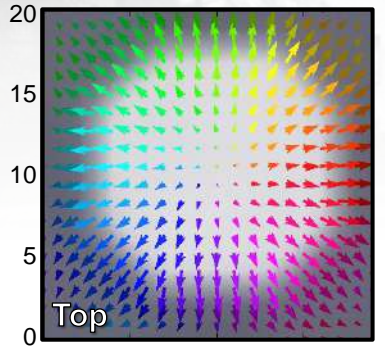


Electric Skyrmions

Pontryagin Density Second Principles–J. Junquera, Univ. Cantabria

Polarization

Pontryagin Density



Polarization

- *Top/bottom planes* → Hedgehog-like (Néel) skyrmion; null rotational, +/- divergence
- *Middle plane* → Combed hedgehog (Bloch) skyrmion; IP $P \parallel$ domain wall, arises from E_D
- *3D polar skyrmion* → Evolution of 2D skyrmions along the film normal

Topology

- Topological structures can be indexed by a *skyrmion number*, defined as

$$N_{SK} = \frac{1}{4\pi} \iint \vec{u} \cdot \left(\frac{\partial \vec{u}}{\partial x} \times \frac{\partial \vec{u}}{\partial y} \right) dx dy$$

N. D. Mermin, *Rev. Mod. Phys.* **51**, 591 (1979)

\vec{u} is the normalized local dipole moment; surface integral over corresponding (001)

Integrand = Pontryagin density

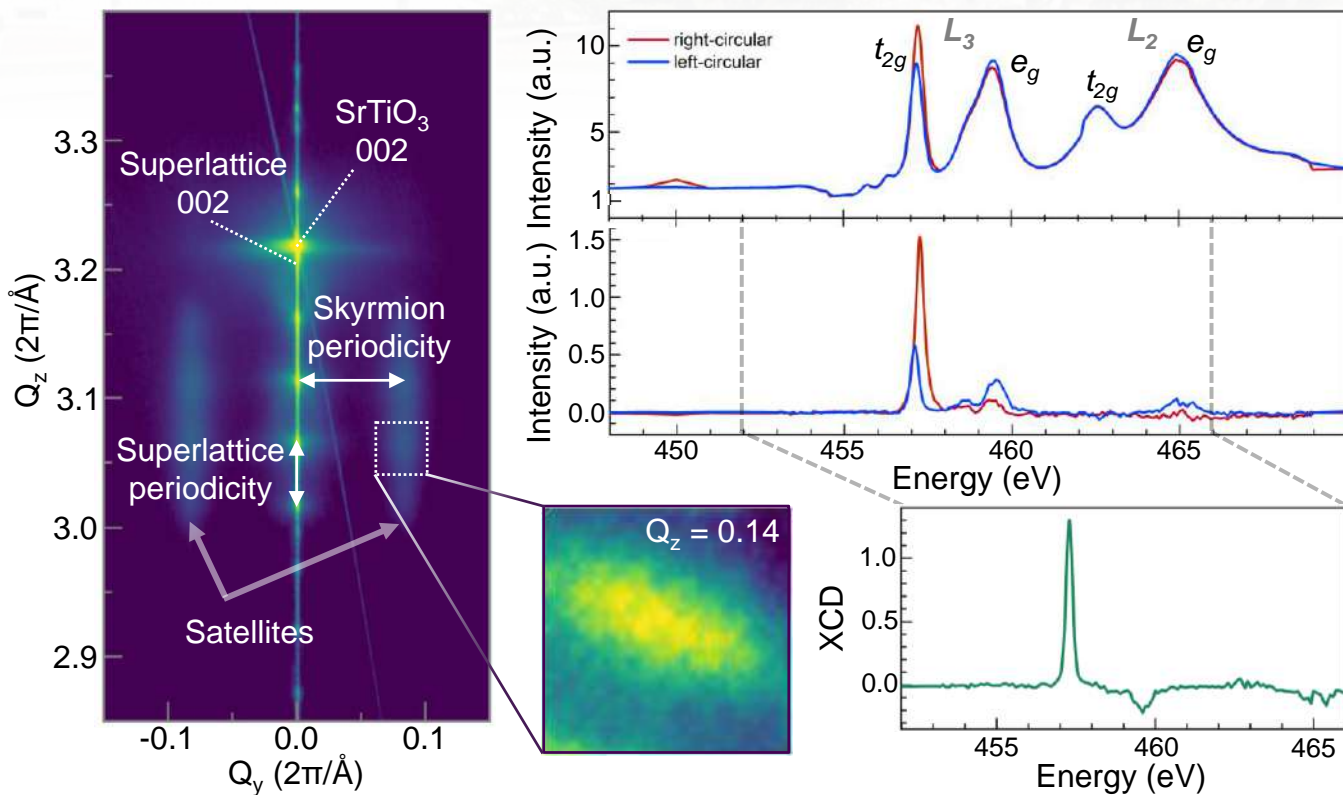
- For this system → $N_{SK} = +1$, an integer that is invariant for every plane
- Even the “Cheetos” manifest $N_{SK} = +1$

First observation of electric (polar) skyrmion

Chiral Electric Skyrmions

Such electric (polar) skyrmions should be chiral...
 Can be probed with *resonant soft X-ray diffraction (ALS)*

- Imaginary line along any direction within the middle plane crosses only Bloch domain walls → Local \mathbf{P} exhibits helical rotation
- Helical \mathbf{P} texture is virtually identical to the helical \mathbf{P} configuration in polar vortex arrays
- Probed at satellite peak, Ti $L_{3,2}$ edge
- Strong circular dichroism at the L_3 edge (corresponding to the t_{2g} states) → Chiral structures; consistent with the presence of Bloch domain walls



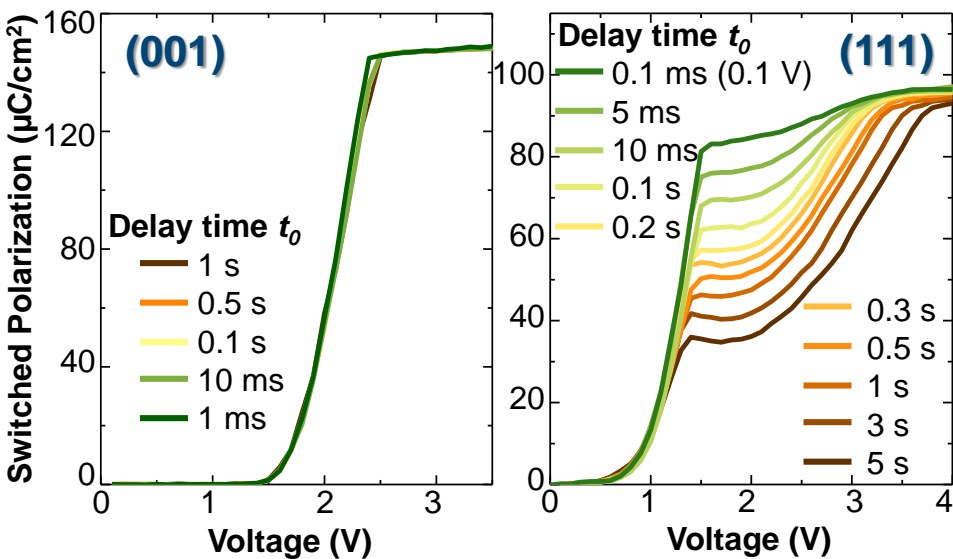
Observation of electric (polar) skyrmions | 3D structure evolves from Néel/Bloch/Néel (top to bottom) | Emergent chiral nature



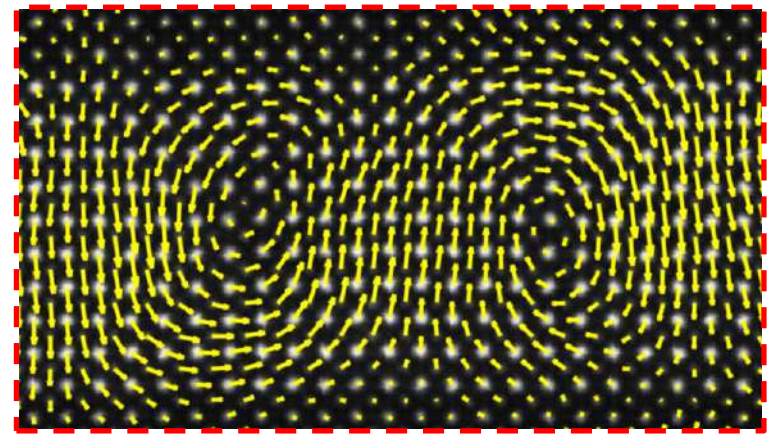
Conclusions and Implications

Accessing emergent phenomena requires novel routes to manipulate and control materials...

Multi-state Switching and Stable Intermediate States



Polar Vortices, Toroidal Order, Phase Competition, Chirality, Electric (polar) Skyrmions



- **(111)-oriented Films** → “Frustration” gives rise to kinetically and elastically-mediated switching, multi-state structures, and the potential for deterministic intermediate states needed for neuromorphic function
- **Superlattices** → Deterministic competition of energies begets novel polarization profiles and emergent properties and function