MULTIFERROICS FROM FIRST PRINCIPLES

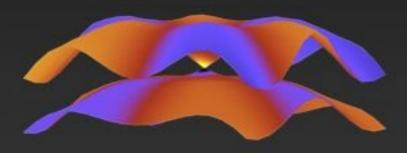


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https://sites.google.com/site/silviapicozzi/







GROUP INTRODUCTION

LOCATION

MATERIALS

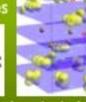
METHODS





Multifunctional/ Coupling between degrees of freedom:





- Organics, hybrid
- Interfaces/surf.
-



- ... but also:
- Symmetry analysis
- Model Hamilt.





FIRST-PRINCIPLES CALCULATIONS: BASICS

Density functional theory

Main theorems

Why are they useful for multiferroics?

Where do they fail?

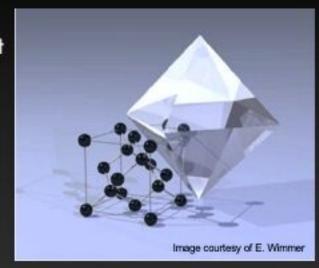




WHAT ARE FIRST-PRINCIPLES USEFUL FOR?

- MACRO

 MICRO: Connect properties with atomic structure
- MODELLING AND UNDERSTANDING: Sort out microscopic mechanisms and physical models.
- COMPUTER-EXPT: Ask "what if" questions.
- MATERIALS DESIGN: Screen ideas for new/modified materials
- THEORY VS EXPERIMENT: Interpret experimental data, compare spectra, etc.



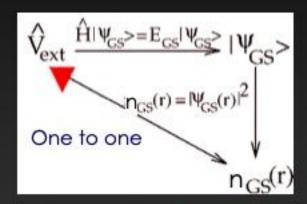
ERRORS... Analyze failures. Ask: Are the approximations appropriate? Can the models
address the complexity of the system? Is the theory appropriate for the key properties?





The basic quantity is not the many-body wave-function but the electronic density n(r)

- Hohenberg-Kohn theorem (1964)
- All properties of the many-body system are determined by the ground state density $n_{GS}(r)$
- Each property is a <u>functional</u> of the ground state density **n**_{Gs}(r) which is written as f [n_{Gs}]
- In particular, the energy is:



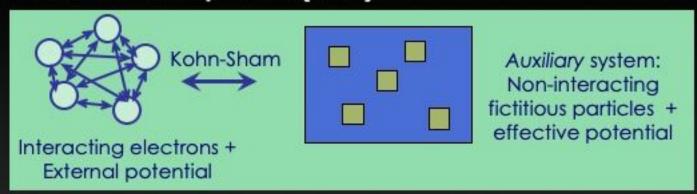
$$E[n(\mathbf{r})] = F[n(\mathbf{r})] + \int V_{\text{ext}} n(\mathbf{r}) d\mathbf{r} = \mathbf{T_e} + \mathbf{U_{ee}} + \int V_{\text{ext}} n(\mathbf{r}) d\mathbf{r} \ge E[n_{GS}(\mathbf{r})]$$

and satisfies a variational principle





Kohn-Sham equations (1965)



The ground state density is required to be the same as the exact density $n_0(\mathbf{r}) = \sum \sum |\psi_i^{\sigma}(\mathbf{r})|^2$

Minimization of E leads to one-particle Kohn-Sham equations for independent particles (soluble):

$$[-1/2 \nabla^2 + V_{\text{eff}}[n(r)]] \psi_i = \varepsilon_i \psi_i$$





Kohn-Sham equations (1965)

$$\{-1/2 \nabla^2 + V_{eff}[n(r)]\} \psi_i = \varepsilon_i \psi_i$$

where:
$$V_{eff}[n (r)] = V_{ext}(r) + V_{H}(r) + V_{xc}[n(r)]$$

V_{ext}(r) is the nuclei (external) potential

$$\bullet V_{H}(\mathbf{r}) = e^{2} \int_{|\mathbf{r}-\mathbf{r'}|}^{\mathbf{n}(\mathbf{r'})} e^{2} \int_{|\mathbf{r}-\mathbf{r'}|}^{\mathbf{n}(\mathbf{r'})} e^{-2} \int_{|\mathbf{r}-$$

is the Hartree potential

•
$$V_{xc}[n(r)] = \frac{\delta E_{xc}}{\delta n(r)}$$

is the (unknown) exchange-correlation potential



- Approximations to the functional Exc
 - Local Density Approximation LDA
 - Assume the functional is the same as a model problem –the homogeneous electron gas
 - E_{xc} has been calculated as a function of density using quantum Monte Carlo methods (Ceperley & Alder)
 - Gradient approximations GGA
 - Various theoretical improvements for electron density that varies in space





OPERATIVELY...

 Structure, types of atoms, guess for input charge

- Solve KS Eqs.
- New Density and Potential
- Self-consistent?
- Output:
 - Total energy, force,
 - Eigenvalues





Initial Guess $n^{\dagger}(r), n^{\downarrow}(r)$

THE GOOD AND THE BAD OF DFT FOR COMPLEX OXIDES

BUT... V_{xc}(r) is approximated "Standard" local density approximation (LDA) designed for a homogeneous electron gas

How to approach strong correlations ?

Beyond-LDA methods:

- LDA+U attempts to incorporate Coulomb repulsions (U)
- Hybrid functionals (mix of "exact-exchange" and LDA)

Hamiltonian modelling:

Extract essential interaction parameters from LDA and construct a model, but also provide a fully independent approach to test the results...





WHAT CAN WE GET OUT OF THE COMPUTER?

Capabilities, formalism	Predicted quantities
Spin-DFT	Electronic structure (DOS, bands,), magnetism (moments, GS spin configuration,)



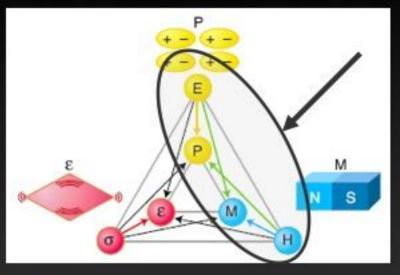
MULTIFERROICS: EXAMPLES FROM FIRST-PRINCIPLES

- Introduction and Classification
- Lone-pair driven
- (Structurally) Improper FE
- (Electronically) Improper FE





MAGNETOELECTRICS MULTIFERROICS: WHAT ARE THEY?



N.A. Spaldin and M. Fiebig, Science 309, 391 (2005)

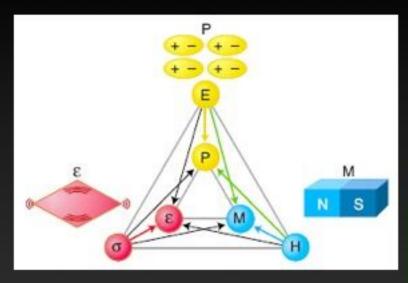
>Ferroic: P, M or ε are spontaneously formed to produce ferroelectricity, ferromagnetism or ferroelasticity

>Multiferroic: coexistence of at least two kinds of long-range ordering

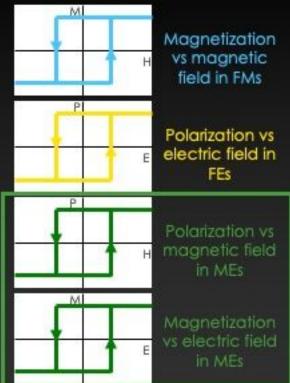




MAGNETOELECTRICS MULTIFERROICS: WHY ARE THEY INTERESTING?



Magnetoelectrics: Control of P (M) via a magnetic (electric) field





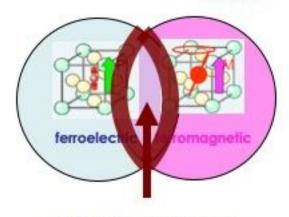


CLASSIFICATION OF MULTIFERROICS

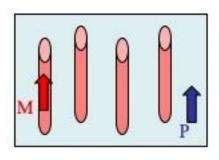


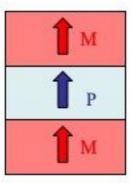
BULK

COMPOSITE



Both magnetic and dipolar order in the same **bulk** material



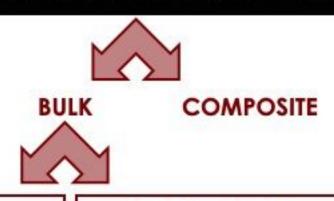


Nanostructures, heterointerfaces of **two different materials** (one **FM** and the other **FE**)

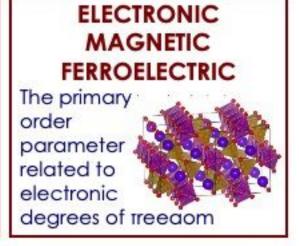




CLASSIFICATION OF MULTIFERROICS



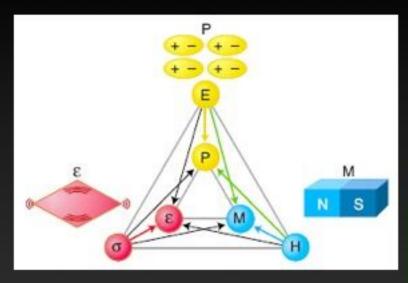
STRUCTURAL MAGNETIC FERROELECTRIC The primary order parameter related to structural instability (either polar or non-polar)



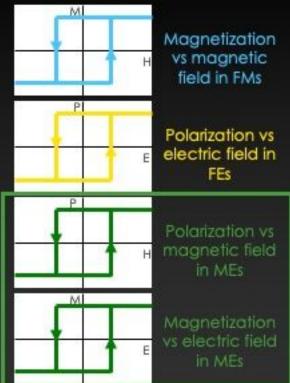




MAGNETOELECTRICS MULTIFERROICS: WHY ARE THEY INTERESTING?

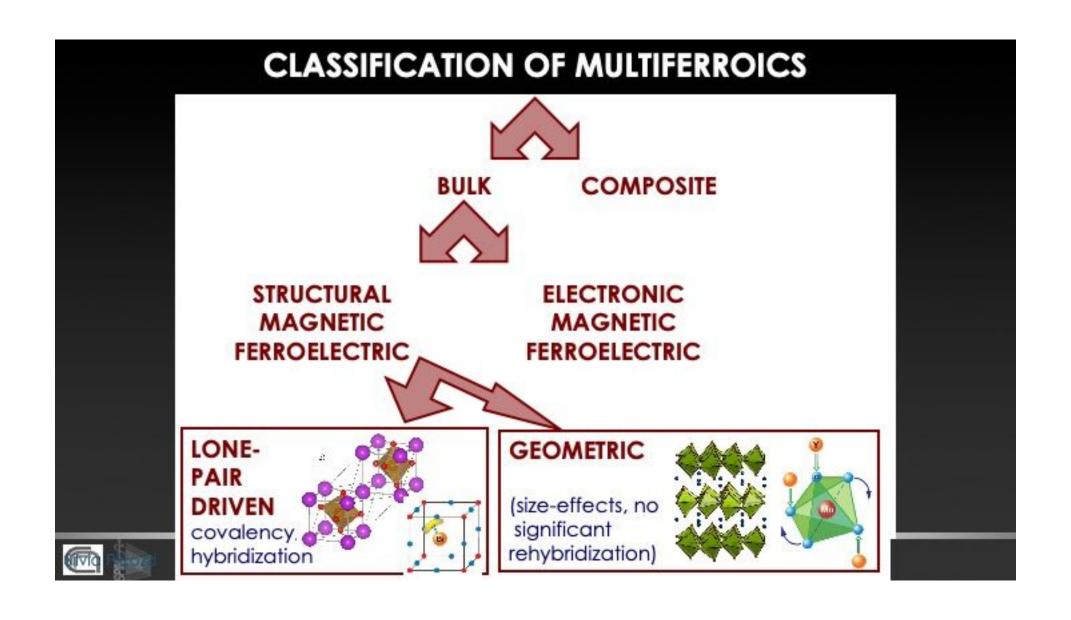


Magnetoelectrics: Control of P (M) via a magnetic (electric) field









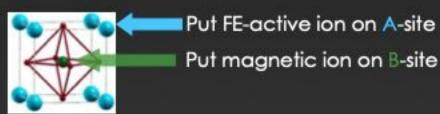
CRITERIA FOR MAGNETISM AND FERROELECTRICITY

- Uncompensated spins form magnetic moments
- Exchange interaction from virtual hopping of electrons between ions
 - To have FM or FiM or AFM, one needs partially filled d-shells!
 - Ferroelectricity requires "do-ness"
 - Ferromagnetism (or FiM- or AFM)
 requires partially filled d-electrons



- B.T. Matthias, New ferroelectric crystals, Phys. Rev. (1949)
- N.A. Hill, Why are there so few magnetic ferroelectrics? J. Phys. Chem. B 104, 6694 (2000)



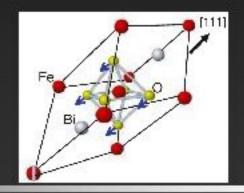




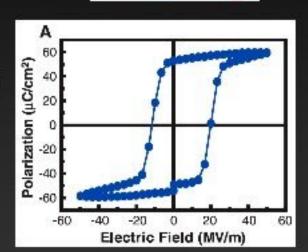


LONE-PAIR DRIVEN MF: THE "HOLY GRAIL, BIFeO₃

- A room-temperature multiferroic: FE and AFM (or weak FM)
- Ferroelectricity from the "stereochemically active lone pair" on Bi³⁺ (cf ammonia, NH₃)
- Magnetism from a 3d transition metal (Fe³⁺, d⁵)
- •Good agreement between theory and expts for P (~100 μC/cm² along [111], ~60 μC/cm² along [001])







J. Wang et al., Science 299, 1719 (2003).

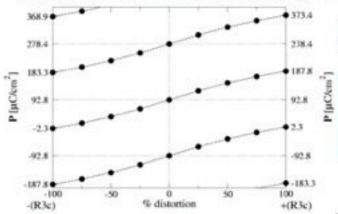






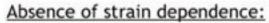
THE "HOLY GRAIL": BiFeO3

Beyond LDA methods: Centrosymmetric reference structure metallic in LSDA Modern theory of polarization: Non-zero P in centrosymmetric structure

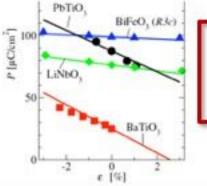


Calculate P = $95 \mu C/cm^2$ along [111]

J.B. Neaton, U.V. Waghmare, C. Ederer, N.A. Spaldin and K.M. Rabe, First-principles study of spontaneous polarization in multiferroic BiFeO₃, PRB 71, 014113 (2005)



Effect of epitaxial strain on the spontaneous polarization of thin film ferroelectrics, C. Ederer and N.A. Spaldin, Phys. Rev. Lett. 95, 257601 (2005)

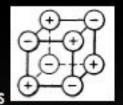


Nicola A. Spaldin's contributions





BiFeO3: MAGNETISM

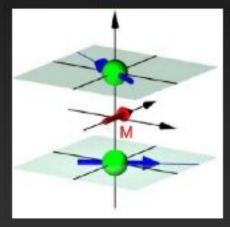


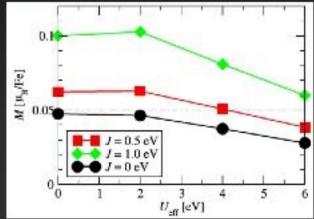
- •Bulk: G-type AFM and cycloidal modulation (λ~640 nm)
- Thin films: the modulation disappears but a weak FM arises

Fe AFM moments are canted by up to ~1° due to Dzyaloshinskii-Moriya interaction

$$E_{\rm DM} = -\frac{1}{2}\vec{D} \cdot (\vec{M}_{\rm Fe1} \times \vec{M}_{\rm Fe2}) = -\vec{D} \cdot (\vec{L} \times \vec{M})$$

 $\vec{M} = \vec{M}_{\rm Fe1} + \vec{M}_{\rm Fe2} \; ; \; \vec{L} = \vec{M}_{\rm Fe1} - \vec{M}_{\rm Fe2}$





C. Ederer and N.A.Spaldin, PRB 71, 060401 (2005)

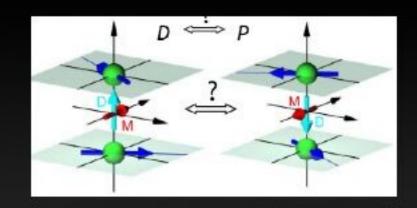




BiFeO3: MAGNETISM

Is the canting coupled to polarization?

Can I switch the weak moment by E-field?



No! Two different modes in BFO:

- 1. Polar displacements along [111]
- 2. Octahedral counter-rotations

.... and DM is related to Oxygen octahedral rotations

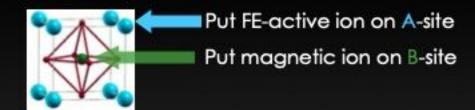






COMBINE FE AND FM: WAY OUT (II)

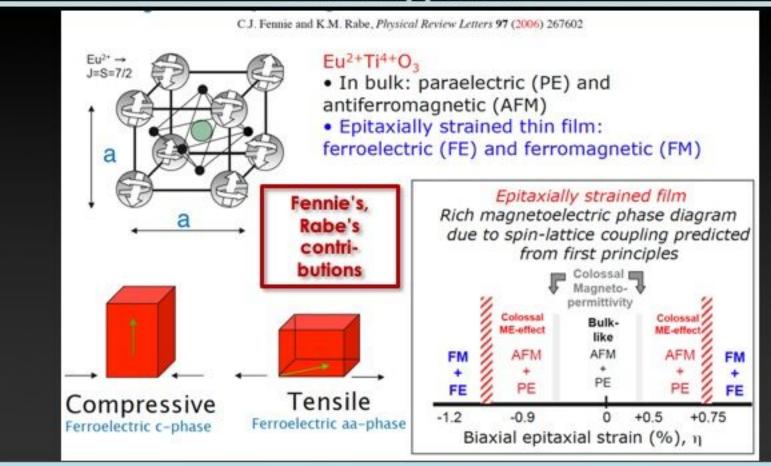
BiFeO₃:







WAY OUT (II): EuTiO3



IMPROPER FERROELECTRICITY IN MAGNETS

What do we mean by "improper ferroelectricity"?

Concepts:

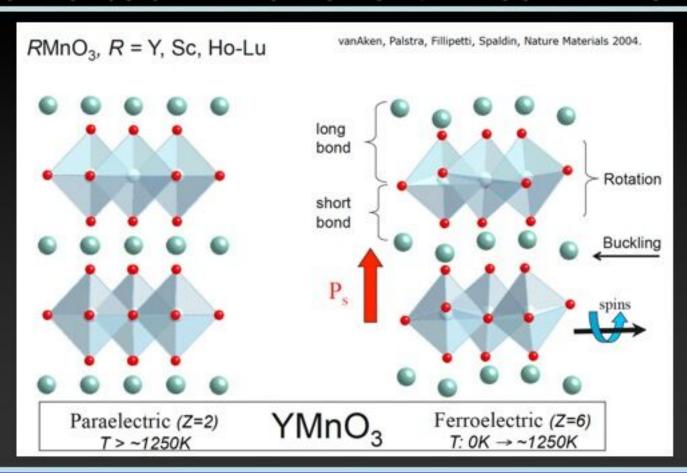
how to break inversion symmetry via coupled structural distortions, spin- or charge-ordering

Examples: manganites (hexagonal vs orthorhombic)

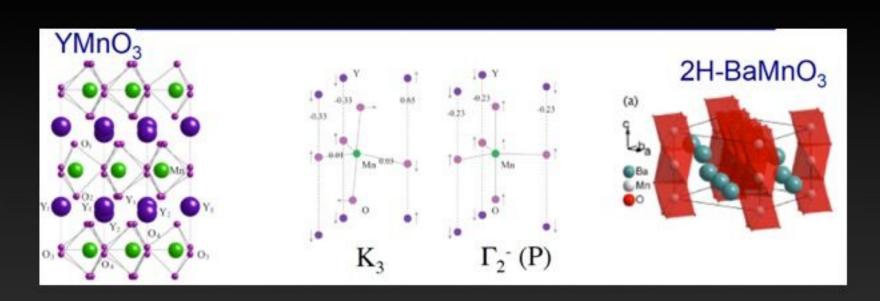




IMPROPER STRUCTURAL FERROELECTRICITY: HEXAGONAL MANGANITES



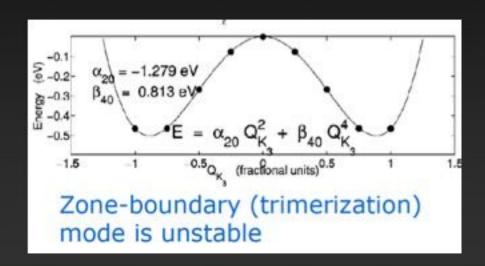
IMPROPER STRUCTURAL FERROELECTRICITY: HEXAGONAL MANGANITES



MnO5 (trigonal bi-pyramids) are rotated and trimerize in the FE state C. Fennie & KM Rabe,
PRB 72, 110103 (2005)
J. Varignon and P. Ghosez,
PRB 87, 140403 (2013)

IMPROPER STRUCTURAL FERROELECTRICITY: HEXAGONAL MANGANITES

⇒ WHY IS IT FERROELECTRIC ?!??!??



RATIONALIZATION WITH LANDAU THEORY

Primary order parameter $\equiv \eta$

Secondary order parameter

where η is "some other mode", e.g. zone-boundary lattice instability, magnetic chiral vector, etc.

Spontaneous polarization P

C. Fennie & KM Rabe, PRB **72**, 110103 (2005) J. Varignon and P. Ghosez, PRB **87**, 140403 (2013)

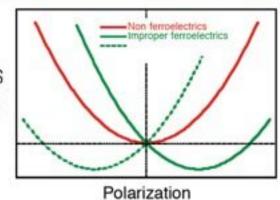
$$\begin{split} \mathcal{F}(\eta,\,P) &= \alpha_P P^2 + \alpha_\eta \eta^2 + \gamma_\eta P \eta^n + \beta P^4 \\ \partial \mathcal{F}/\partial P &= 2\alpha_p P + \gamma_\eta \eta^n + 4 \; \beta P^3 = 0 \end{split}$$

 $P_{eq} \sim - \eta^n$

Once primary OP becomes nonzero, a polarization is induced

IMPROPER FERROELECTRICITY: RECAP

$$\mathcal{F}(\eta, P) = \alpha_{P}P^{2} + \alpha_{\eta}\eta^{2} + \frac{\partial \theta}{\partial \theta}$$
$$+ \gamma_{\eta}P\eta^{n} + \beta P^{4}$$
$$= faintness index$$



- P not intrinsically unstable but slave of another unstable degree of freedom (structural or other) φ.
- P coupling at linear order with φ → shift of the well.
- Other exponent n (« faintness ») possible (n = 1 : pseudo-proper)
- · No anomalous Born Effective Charges
- Ferroelectric ? Yes, but switching P requires switching φ ...
- No divergence of the dielectric constant

IMPROPER FERROELECTRICITY IN HEXAGONAL MANGANITES

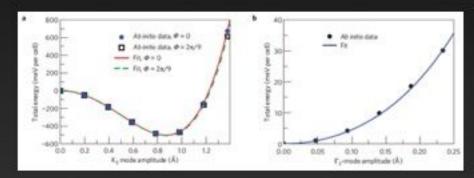
Expand energy to fourth order in the primary K_3 and secondary P order parameters:

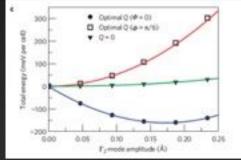
(note energy expansion simplified for pedagogy)

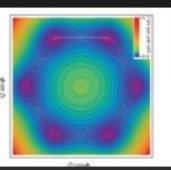
Fennie and Rabe, Physical Review B 72, 100103 2005

$$F(K_3, P) = \alpha_P P^2 + \alpha_k K_3^2 + \gamma_\eta P K_3^3 + \beta P^4$$

$$\Rightarrow P \sim \gamma_\eta K_3^3$$







Extraction of model parameters from ab-initio (K_3 : trimerization mode, Γ_2 : polar mode). S. Artyukhin et al, Nat. Mater. 13, 42 (2014).

BREAKING INVERSION SYMMETRY IN MAGNETS

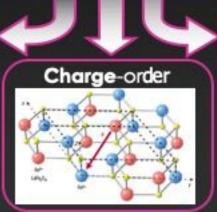
Conventional

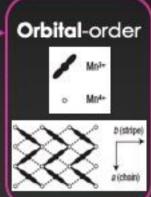
FERROELECTRICITY - no Inversion Symmetry

- "Proper"
- Ionic displac. break inversion symmetry (IS)
- "Covalency"-driven
- "Improper"
- Electron degrees of freedom break IS
- "Correlation"-driven



Spin-order (some AFM or "spiral")



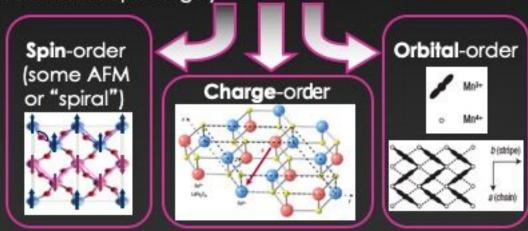






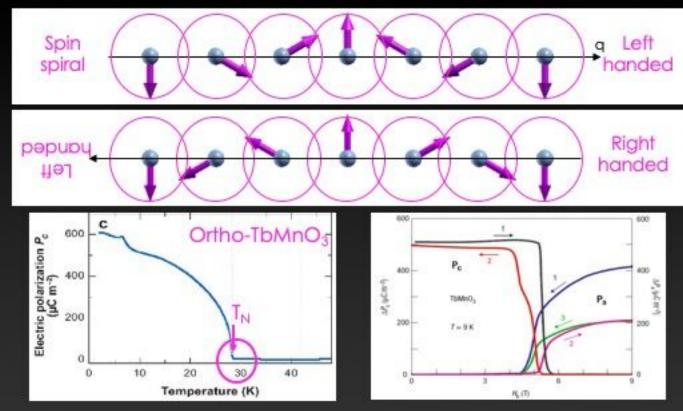
Main advantages over proper multiferroics:

- displacements/switching involve electrons rather than ions
 - ⇒ switching should be much faster
 - ⇒ better as for "fatigue"
- especially for spin-induced ferroelectricity
 - ⇒ magnetoelectric coupling should be much stronger (as magnetism and ferroelectricity share the same microscopic origin)





HOW MAGNETIC ORDERING CAN BREAK INV. SYM.?



T.Kimura et al., Nature 425, 55 (03); S.W.Cheong and M.Mostovoy, Nature Mater. 6, 13

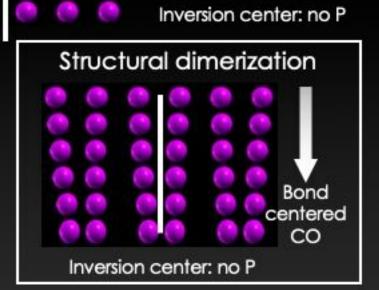




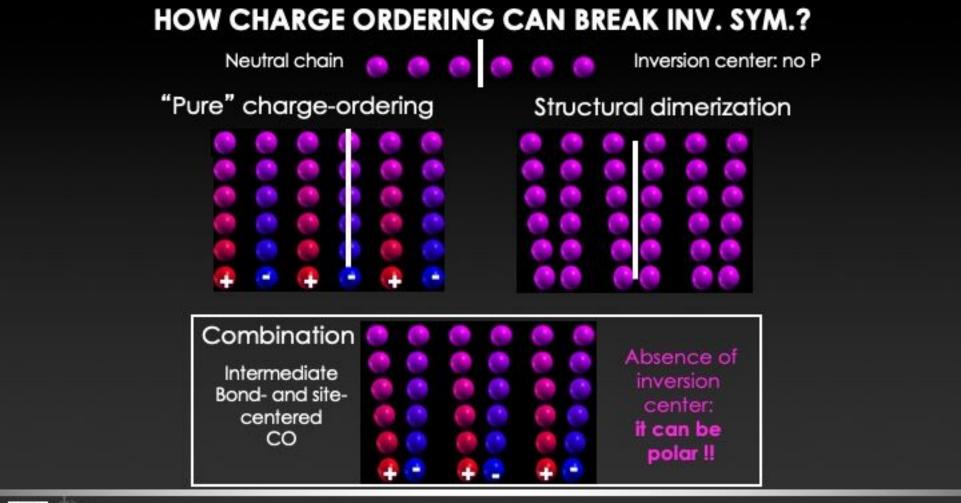
HOW CHARGE ORDERING CAN BREAK INV. SYM.?

"Pure" charge-ordering
Site centered

Inversion center: no P

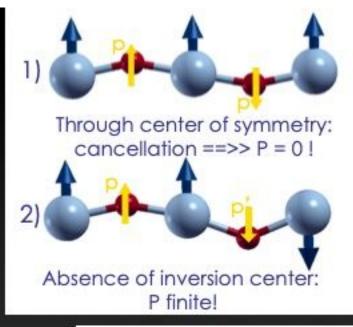






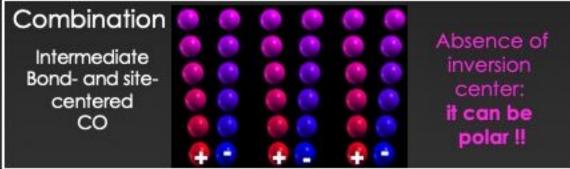






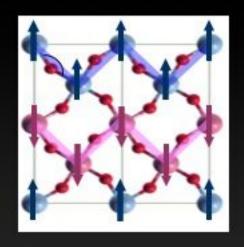
... but these are
just "sketches"...
In practice we have to find
materials where these
"local" dipoles
are periodically repeated

⇒ polar space groups









E-TYPE MANGANITES: ELECTRONIC AND IONIC FERROELECTRICITY

•In collaboration with:

K. Yamauchi (now at Osaka)



I. A. Sergienko, E. Dagotto (Oak Ridge Natl. Lab, Univ. Tennessee, TN)

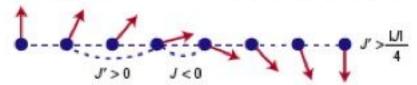






FRUSTRATION IN MAGNETS

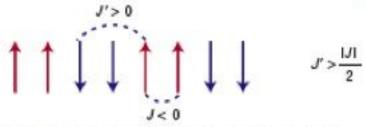
Frustrated spin chains with the nearest-neighbour FM and next-neighbour AFM interactions J and J´.



The spin chain with isotropic (Heisenberg)

$$H = \Sigma_n[J S_n \cdot S_{n+1} + J' S_n \cdot S_{n+2}].$$

For J'/|J| > 1/4 its classical ground state is a magnetic spiral.



The chain of Ising spins $\sigma_n = \pm 1$, with energy

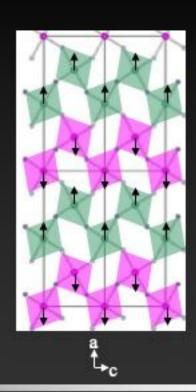
$$H = \sum_{n} [J \sigma_{n} \sigma_{n+1} + J' \sigma_{n} \sigma_{n+2}]$$

has the up-up-down-down ground state for J'/J > 1/2.

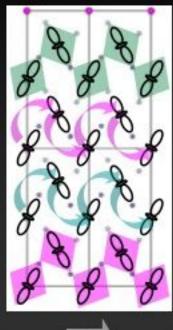


WHY THE AFM-E SHOULD BE FERROELECTRIC?

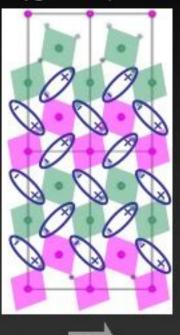
• "Electronic" mechanisms



e_g Orbital Ordering



Oxygen inequivalency

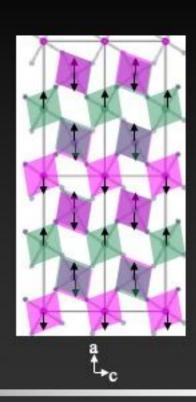




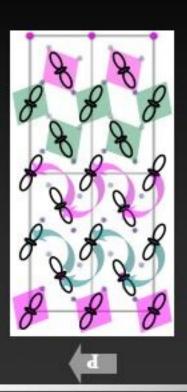


WHY THE AFM-E SHOULD BE FERROELECTRIC?

• "Switching" mechanisms: change direction of some spins





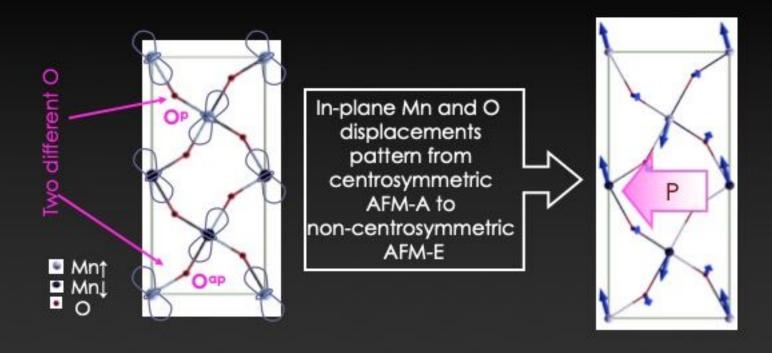






WHY THE AFM-E SHOULD BE FERROELECTRIC?

• "Structural" contributions: Magnetostriction



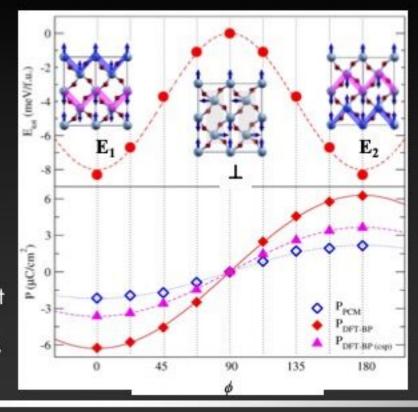




ORTHO-HOMNO3 AS A MAGNETICALLY DRIVEN FERROELECTRIC

- First ab-initio calculation of P driven by AFM*
- P is ~few μC/cm² (highest among magnetic improper ferroelectrics)
- FE switching path via spin-rotations
- Dual nature of P in real compounds: ionic displacements and electronic/magnetic effects are both important

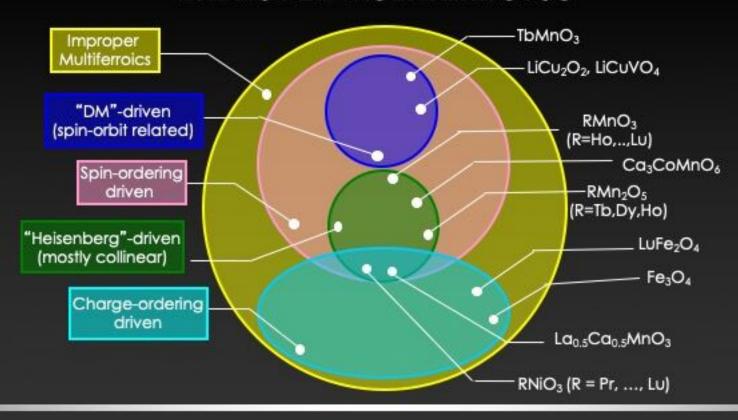
* S. Picozzi, K. Yamauchi, B. Sanyal, I. Sergienko, E. Dagotto, PRL 99, 227201 (2007)





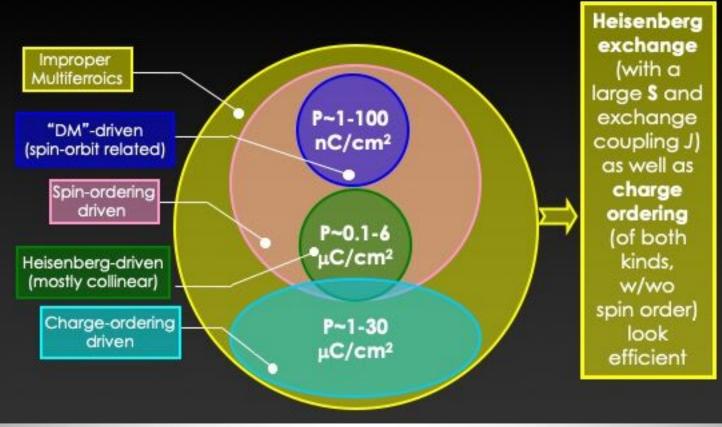


CLASSIFICATION OF IMPROPER MULTIFERROICS

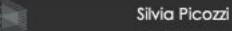










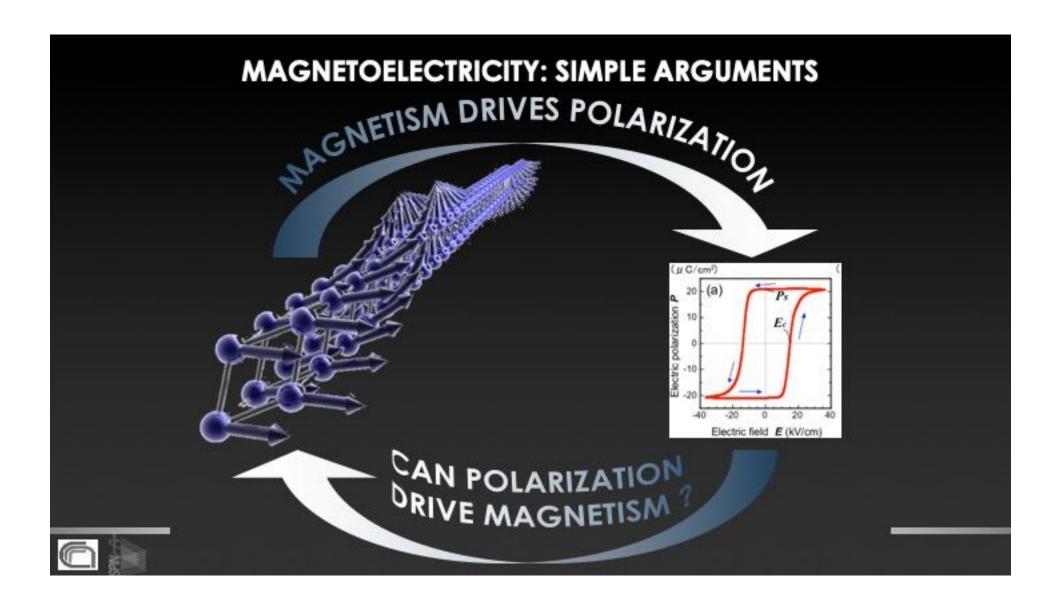


OTHER MECHANISMS OTHER MATERIALS

- 1. Can we drive magnetism with an electric field?
- 2. Can we use organic or metal-organic frameworks?



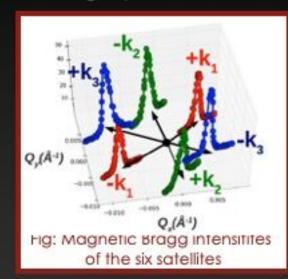




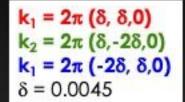
X-ray imaging of cycloidal magnetic domains in ferroelectric monodomain BiFeO₃

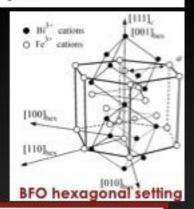
R. D. Johnson, 1, 2 P. Barone, 3 A. Bombardi, 4 R. J. Bean, 5 S. Picozzi, 3 P. G. Radaelli, Y. S. Oh, S-W. Cheong, and L. C. Chapon

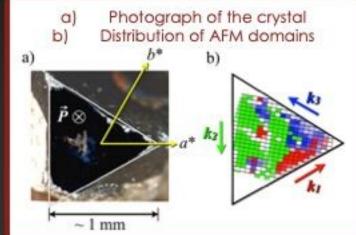
Hard X-ray Magnetic Scattering (DIAMOND, UK): High space and momentum resolution



Imaging of 3 large (up to 500 µm) magnetic domains for k₁,k₂,k₃







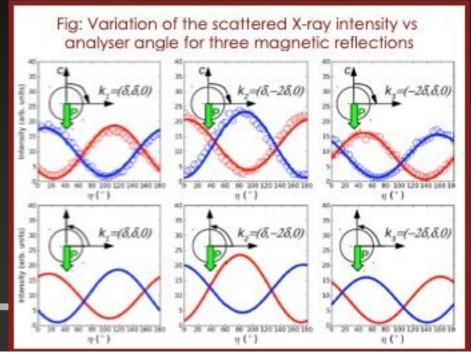


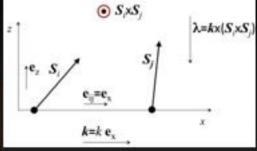


DETERMINATION OF MAGNETIC POLARITY λ

X-ray Magnetic Scattering with circ. pol. Light

⇒ Determination of absolute rotation direction of magnetization









All magnetic configurations rotate clockwise!!



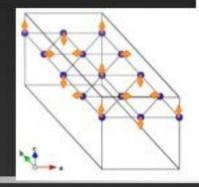


MICROSCOPIC ORIGIN: DFT

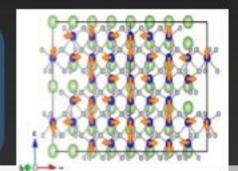
(Real) Cycloid modulation 640 Å ⇒ Reduce unit cell in DFT: 2ax4bxc (240 atoms)

76	τ (Å)	$P_c \left(\mu C/cm^2\right)$	$\Delta E (meV) (Fe)$
FE↑	0.668	105.17	-2.34
PE	0	0	0
FEL	-0.668	-105.17	2.34

TABLE I. DFT results obtained for U=5 eV, J=1 eV. The energy difference is defined as $\Delta E = E_{CW} - E_{CCW}$. FE† and FE↓ are characterized by opposite collective displacements, τ , respectively upward and downward, of Bi sublattice with respect to O layers perpendicular to c axis.



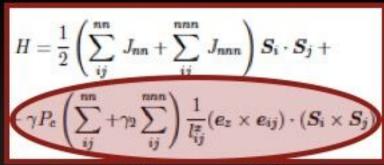
The sign of FE polarization stabilizes the magnetic polarity of the cycloid. For PE, CW and CCW states are degenerate







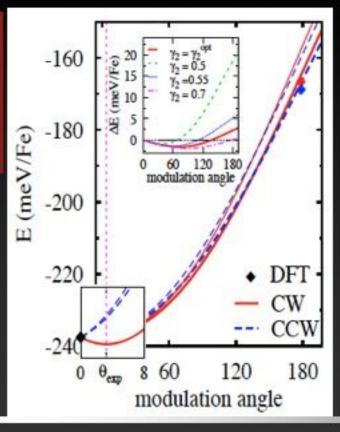
MODEL HAMILTONIAN STUDY



COUPLING TERM:

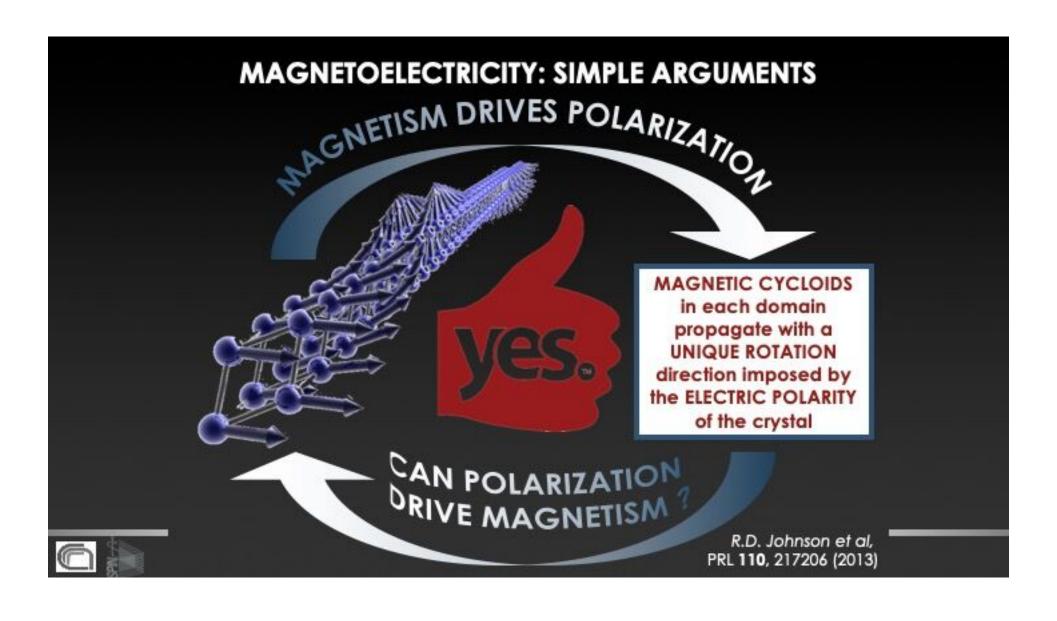
ZIALOSHINSKII-MORIYA LIKE

The energy favored magnetic polarity depends on modulation angle ⇒ Importance of 2nd nn to reproduce expts ⇒ γ ~ 2.4 x 10⁻⁴ V

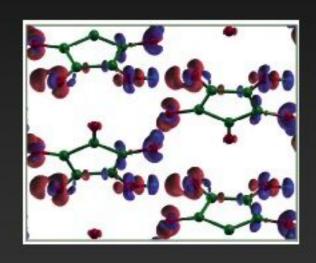


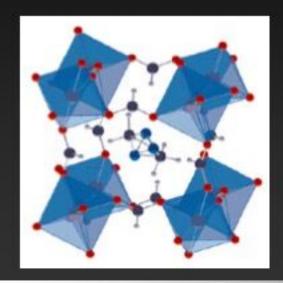






... NOT ONLY OXIDES: ORGANICS & HYBRIDS





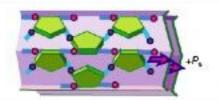


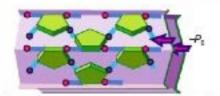


PROTON TRANFER: EFFICIENT SOURCE OF P

Vol 463 11 February 2010 doi:10.1038/nature08731

nature

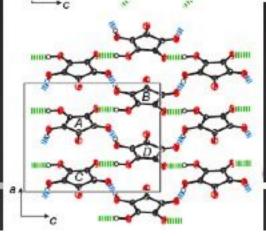


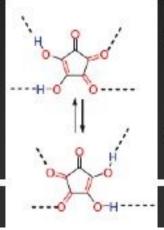


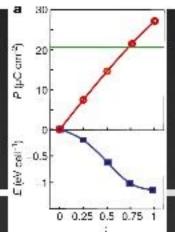
LETTERS

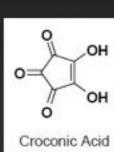
Above-room-temperature ferroelectricity in a single-component molecular crystal

Sachio Horiuchi¹, Yusuke Tokunaga², Gianluca Giovannetti^{3,4}, Silvia Picozzi³, Hirotake Itoh², Ryo Shimano^{2,5}, Reiji Kumai¹ & Yoshinori Tokura^{1,2,6}





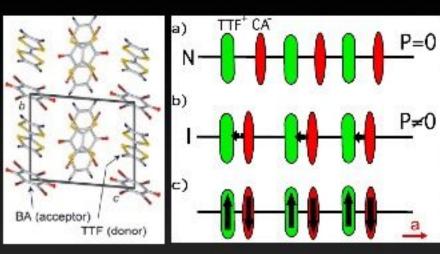


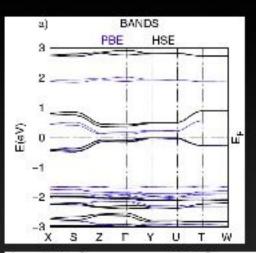




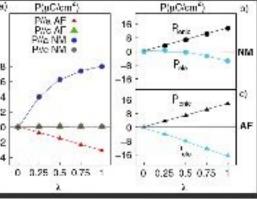


TTF-CA: SPIN-PEIERLS AS A SOURCE OF P?



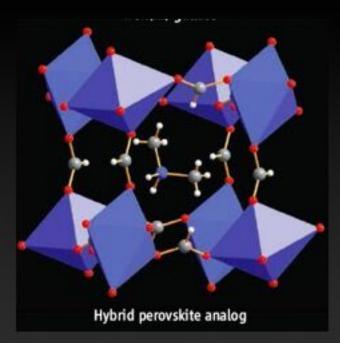


- •SPIN PEIERLS: One-dimensional Heisenberg spin 1/2 chain ==>> instability to a dimersinglet (gain of symmetric exchange)
- TTF-CA: Under the neutral-lonic transition

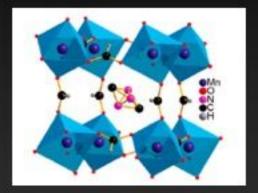




METAL-ORGANIC FRAMEWORKS



Crystalline hybrid materials like Metal Organic Frameworks (MOFs) are very attractive materials for gas storage, drug delivery, catalysis, optics, and magnetism



Hybrid Improper Ferroelectricity in a Multiferroic and Magnetoelectric Metal-Organic Framework

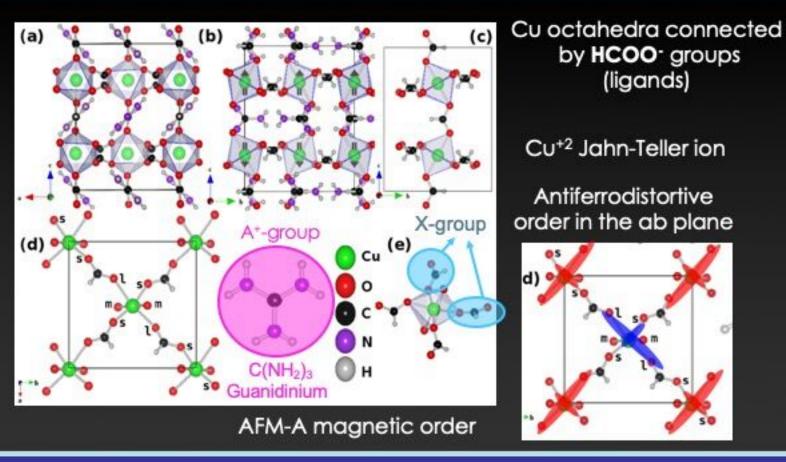
Adv. Mater. 2013, 25, 2284-2290



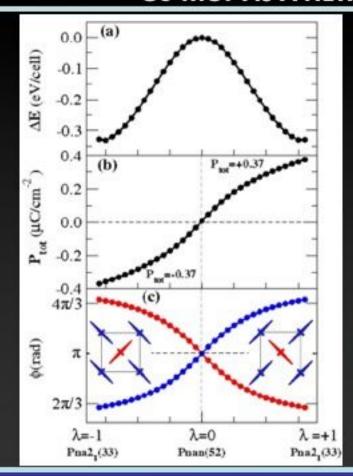


A. Stroppa,* P. Barone, P. Jain, J. M. Perez-Mato, and S. Picozzi

METAL-ORGANIC FRAMEWORKS



Cu-MOF AS A NEW MULTIFERROIC



λ amplitude of the polar distortion:

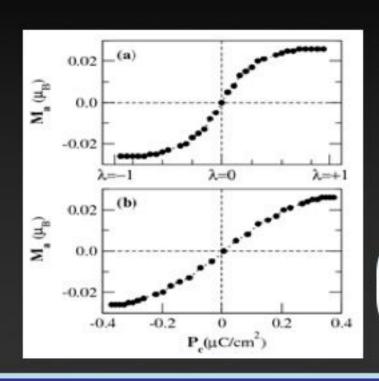
 λ =0 paraelectric state (P=0); λ =+/- 1 ferroelectric (FE) state (P=0.37 μ C/cm2).

NB: The AFD order is non-polar in usual inorganic compound (like KCuF3)

In Cu-MOF AFD and FE are clearly correlated!

Cu-MOF AS A NEW MULTIFERROIC

Symmetry analysis: Coupling of the type $M_aP_cL_c$ \Rightarrow Weak-FM component is allowed in Cu-MOF and coupled to FE order!



Ab-initio calculations fully confirm what expected by symmetry

In Cu-MOF, a magnetic field can couple to weak-FM component and can reverse FE polarization (and viceversa: an electric Field can switch weak-moment)

ELECTRICAL CONTROLOF MAGNETIZATION!

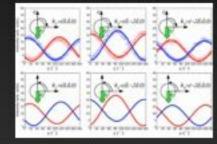
TAKE HOME MESSAGES

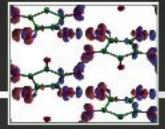
- First principles calculations can give valuable insights into mechanisms and quantitative reliable estimates for different materials
- Very different microscopic origins for improper ferroelectricity
- Heisenberg exchange striction seems a mechanism able to drive a large polarization!



- Charge ordering is an efficient mechanism!
- **MAGNETOELECTRICITY:** can polarization drive magnetism? The case of BiFeO₃ spin cycloid





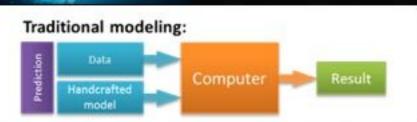








FUTURISTIC OUTLOOK: MACHINE LEARNING?



Can we use DFT data to train a

Machine Learning Algorythm
to predict when a material is FE
or AFE, to go to high
time/space scales, to design
room temperature MF?



1 PhD and 1 post-doc position opening: pls contact me!





